

# Training Machine Learning Models With Causal Logic

Ang Li, Suming J. Chen, Jingzheng Qin, Zhen Qin

Google

Mountain View, California, USA

{angliangli,suming,jzq,zhenqin}@google.com

## ABSTRACT

Machine-learning (ML) models are ubiquitously used to make a variety of inferences, a common application being to predict and categorize user behavior. However, ML models often suffer from only being exposed to biased data – for instance, a search ranking model that uses clicks to determine how to rank will suffer from position bias. The difficulty arises due to user feedback only being observed for one treatment and not existing counterfactually for other potential treatments. In this work, we discuss a real-world situation in which a binary classification model is used in production in order to make decisions about how to treat users. We introduce the model as well as the limitations of our modeling approach, and show that by using counterfactual selection criterion we can improve upon the current modeling process and do a better job classifying users. Following, we propose a causal modeling method in which we can take the existing data and use it to derive bounds that can be used for objective function modification in order to incorporate counterfactual learning into our training process. We demonstrate the effectiveness of this approach in a real-world setting.

## CCS CONCEPTS

• **Mathematics of computing** → **Causal networks.**

## KEYWORDS

counterfactual learning

### ACM Reference Format:

Ang Li, Suming J. Chen, Jingzheng Qin, Zhen Qin. 2020. Training Machine Learning Models With Causal Logic. In *Proceedings of ACM (IID 2020)*. ACM, New York, NY, USA, 5 pages. <https://doi.org/10.1145/nnnnnnn.nnnnnnn>

## 1 INTRODUCTION

Correctly predicting and categorizing user behavior is critical in many industry areas. For example, in online advertising [3, 8, 11, 14], there are companies whom are interested in identifying users who would only click on an advertisement if and only if the said advertisement is highlighted. Another example lies in customer relationship management [6, 12], where it’s desirable to predict which customers are about to churn but are likely to change their minds if enticed towards retention. A common difficulty in predicting and

categorizing behavior arises due to user feedback only being observed for one treatment and not defined counterfactually in terms of what the individual would do under hypothetically unrealized conditions. For example, if we see that a user clicked on a promoted advertisement, we don’t know if they would have clicked on that advertisement had it not been highlighted.

To better categorize user behavior for prediction, it’s useful to classify individual behavior into four response types, labeled complier, always-taker, never-taker, and defier [1, 2]. Compliers are individuals who would respond positively had they been encouraged and negatively if not encouraged. Always-takers and never-takers always respectively respond positively/negatively whether or not they get encouragement. Defiers are individuals who response negatively if encourage and positively if not encouraged.<sup>1</sup> Commonly, unit selection is used to target compliers since that would result in the most effective treatment.

[7] treats the unit selection problem using the structural causal model (SCM) [10] in order to take into account the counterfactual nature of the desired behavior, similar to [4, 5], and found that unit selection can derive selection criteria that allows for ways to decide which group to expose to a treatment in order to yield greater benefit than standard methods. In the work of [7], they found that the unit selection problem entails two sub-problems of evaluation and search, and propose a solution for the evaluation sub-problem – theoretically useful, but often impractical in a real world setting where treatments need to be made at the individual level.

In this work, we propose a method in which the search sub-problem can be approximately solved, by show that even computing group-wise attributes (e.g. a label for a group of users) with counterfactual unit-selection derived bounds, we can modify the learning objective function in order to train a better performing decision-making model by providing counterfactual information to the training process. We applied this methodology to an application where the goal is to balance search quality with resource utilization, and saw an improvement over the standard training procedure.

This paper is structured as follows: we first describe the real-world motivating example for this approach and go over the background of the production model. Next, we discuss some needed background for the counterfactual logic associated with SCM and frame it in the context of our motivating example. Following, we present our derived methodology of modifying the training objective to incorporate additional counterfactual logic and follow up with the experiment results of our newly trained model.

## 2 REAL-WORLD MOTIVATING EXAMPLE

GMail is an email service and Google Drive is a file sharing and storage system – there is a search bar in GMail that shows “instant”

<sup>1</sup>For instance, a user who would click an advertisement if only it wasn’t promoted.

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for components of this work owned by others than ACM must be honored. Abstracting with credit is permitted. To copy otherwise, or republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee. Request permissions from [permissions@acm.org](mailto:permissions@acm.org).

*IID 2020, April 2020, Taipei*

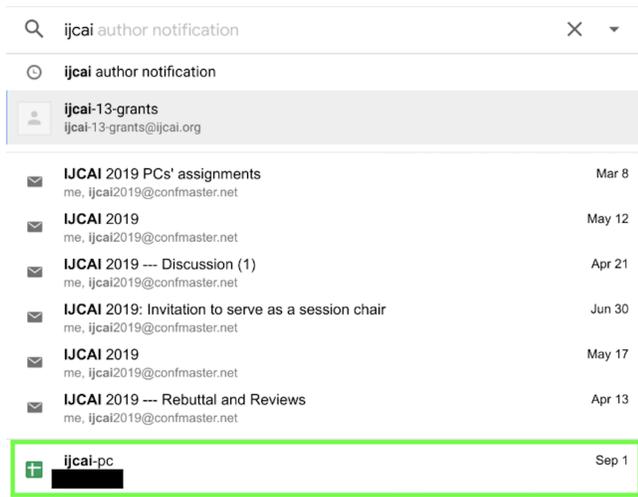
© 2020 Association for Computing Machinery.

ACM ISBN 978-x-xxxx-xxxx-x/YY/MM... \$15.00

<https://doi.org/10.1145/nnnnnnn.nnnnnnn>

results, where every keypress may trigger different email search results to render. In addition to this, the search bar may also show file search results from users’ Google Drive accounts. An example of this is shown in Figure 1.

Since not all users who use Gmail necessarily will use Drive, a decision that needs to be made is whether or not to suppress that additional call to Drive, especially if there is a strong belief user will not click that link, as this will allow for resource-saving. For consistent user experience, post-deciding whether or not to suppress that section, we lock that decision for a window of time. The more users we enable the section for, the more *effective* the search system is, whereas the fewer users we enable the section for, the more *efficient* our search system becomes, thus putting us in a position to trade off effectiveness and efficiency, similar to [13].



**Figure 1: Example search bar and with suggestions and search results. Results from both Gmail and Google Drive are shown, with Drive results bounded in the green box.**

We developed a machine-learned model in order to decide whether or not to suppress that section. Initially there was a heuristic method set up to enable and disable Gmail non-native section based on the statistics of user’s past activities (how often they click on the non-native section, how often they click on Drive documents). For example, Gmail non-native section will be disabled for users who have no Drive activities in the past  $X$  days; once they have clicks on Gmail non-native section, Gmail non-native section will be shown for the next  $Y$  days, etc.

The heuristic model was replaced by a machine-learned model that is modeled as a trade-off between clicks and resources available. Note that because of the method in which initial heuristic model was deployed, offline training and evaluation data is *biased* – if the heuristic rule turns the non-native section off for a user, we will not get any clicks on the non-native section, which is exactly what was used before to make the decision of whether to enable/disable the non-native section.

At a high level, we model this as a *binary classification* problem where we are determining which users should and shouldn’t have their non-native results suppressed, with an objective that

considers both click and resources-used (using the logged number of keypresses per-search as a proxy). Each training data point is at user level, with the input features being the frequency of user activities (e.g. the number of views, edits, creates on Drive documents). At serving time, our model needs to decide whether or not to suppress the user’s non-native results for the day.

To get labels for the training data, we get the *click* and *keypress* on the 1 holdout day (we generate 7 datasets with the holdout day being each weekday, the 7 datasets are merged into one final dataset). The per-user objective function, given positive hyperparameters  $\alpha$  and  $\beta$  is:

$$((\alpha * \text{click} - \text{keypress}) > 0 ? 1 : 0) \tag{1}$$

which we treat as the objective function for binary classification, where each example is weighted by:

$$\beta * \text{abs}(\alpha * \text{click} - \text{keypress}) \tag{2}$$

This results in an intuitive setting: If a user has many clicks but a low number of key-presses, then the weight in Equation 2 is high and the label is positive, which means it’s especially important for the model to predict this user as positive during training (turn on the non-native section). If a user does not have many clicks but has a lot of keypresses, the weight is also high and label is negative, the model is more likely to disable the non-native section for the user, saving resources while not losing clicks.

This model led to performance gains, but suffered from the bias problem. There are methods which allow for running experiments, including with contextual bandit approaches [8], in order to collect unbiased data to train a fairer model, i.e. to set some kind of forced exploration to have a newly trained model make a different decision. However, these existing methods are often not practical since they would harm user experience (exposing to multiple confusing treatments). This motivates us to look for alternative methods in order to more accurately predict whether or not a user really needs the non-native section enabled.

### 3 BACKGROUND

#### 3.1 Counterfactual Logic

In this section, we review the counterfactual logic [4, 5, 10] associated with Pearl’s SCM, which is used in the remainder of this paper. The basic counterfactual statement associated with model  $M$  is denoted by  $Y_x(u) = y$ , and stands for: “ $Y$  would be  $y$  had  $X$  been  $x$  in unit  $U = u$ .” Let  $M_x$  denote a modified version of  $M$ , with the equation(s) of set  $X$  replaced by  $X = x$  (i.e., all edges that go into  $X$  have been removed). Then, the formal definition of the counterfactual  $Y_x(u)$  is as follows:

$$Y_x(u) \triangleq Y_{M_x}(u) \tag{3}$$

In words, the counterfactual  $Y_x(u)$  in model  $M$  is defined as the solution of  $Y$  in the “modified” submodel  $M_x$ . In [4, 5], a complete axiomatization of structural counterfactuals, embracing both recursive and nonrecursive models, is given.

Equation (3) implies that the distribution  $P(u)$  induces a well-defined probability for the counterfactual event  $Y_x = y$ , written as  $P(Y_x = y)$ , which is equal to the probability that a random unit  $u$  would satisfy the equation  $Y_x(u) = y$ . Therefore, the probability

of the event “Y would be  $y$  had X been  $x$ ”,  $P(Y_x = y)$ , is well-defined and  $P(Y_x = y)$  is also equivalent to  $P(Y = y|do(X = x))$ .  $P(Y = y|do(X = x))$  can be interpreted as experimental data [9]. With the same reasoning, the SCM model assigns a probability to every counterfactual or combination of counterfactuals that are defined using the variables in SCM.

Using the above formal language for the counterfactual expression, all events involving a counterfactual scenario can be well defined, because the event represented by the subscript does not actually occur. For example,  $P(Y_x = y|X = x')$  defines the probability of the event “Y would be  $y$  had X been  $x$  if we observed  $X = x'$ ” (note that  $x$  and  $x'$  are counterfactual scenarios),  $P(Y_x = y, Y_{x'} = y')$  defines the probability of the event “Y would be  $y$  had X been  $x$  and Y would be  $y'$  had X been  $x'$ ” (note that  $x$  and  $x'$  is a counterfactual scenario;  $y$  and  $y'$  is a counterfactual scenario), and  $P(Y_x = y|X = x', Y = y')$  defines the probability of the event “Y would be  $y$  had X been  $x$ , if we observed  $X = x'$  and  $Y = y'$ ”.

In the rest of the paper, let  $y$  denote that the user would click the non-native link and  $y'$  denotes that the user would not click the non-native link. Let  $x$  denote that the non-native link is shown to the user and  $x'$  denotes that the non-native link is not shown to the user. As such, we use  $y_x$  to denote the event  $Y_x = y$  (user would click if non-native section was shown),  $y_{x'}$  to denote the event  $Y_{x'} = y$  (user would click if non-native section wasn't shown – meaning the user had to go to Drive app to click),  $y'_x$  to denote the event  $Y_x = y'$  (user would not click if non-native section was shown), and  $y'_{x'}$  to denote the event  $Y_{x'} = y'$  (user would not click if non-native section wasn't shown).

## 4 CAUSAL METHODOLOGY

### 4.1 Motivation

Unit selection based on counterfactual logic has been proven in [7] to be effective in the unit selection problem, where a decision maker must determine which group of users should receive an experimental treatment. We draw inspiration from this to derive a new method that allows for *extending* a training objective function to incorporate unit selection counterfactual logic.

With the previously introduced notation and groups defined in [1, 2], we have the following individuals to consider for our decision-making problem:

- Complier ( $y_x, y'_{x'}$ ): Users who would access the Drive file if and only if they have the non-native link.
- Always-taker ( $y_x, y_{x'}$ ): Users who would access the Drive file whether or not they have the non-native link.
- Never-taker ( $y'_{x'}, y'_{x'}$ ): Users who would not access the Drive file whether or not they have the non-native link.
- Defier ( $y_{x'}, y'_x$ ): users who would access the Drive if and only if they have no non-native link.

By modeling users this way, we can see that it's optimal to provide non-native section to the always-taker (as the first priority) and then non-native section to compliers as a short-cut (as second priority if there are enough resources). Never-takers should clearly

never be shown the non-native section, and defiers in this scenario we believe to be not practical or necessary to consider.<sup>2</sup>

Note that the previously introduced ML model was not trained on this kind of counterfactual information. The key takeaway here is that although we can never know the response type for a particular user, we can bound their probabilities if we have experimental and observational data  $P(y_x)$ ,  $P(y_{x'})$ , and  $P(x, y)$ .

### 4.2 Causal Model

Our objective is to find a subset of users that maximizes the benefit associated with the resulting mixture of compliers, defiers, always-takers, and never-takers. Our ideal objective, then, should be

$$\alpha * \text{click} - \text{keypress} + \beta * P(y_x, y'_{x'}) + \gamma * P(y_x, y_{x'}) + \theta * P(y'_x, y'_{x'}) + \delta * P(y'_x, y_{x'}) \quad (4)$$

Note that in this application, we set

$$\beta > \gamma > 0 = \delta > \theta$$

to indicate that always-taker is the first priority and complier is the second priority.  $\delta = 0$  is set to express that for this scenario we don't consider defiers to be a valid group to consider. We would set  $\theta$  to be some negative value to penalize never-takers.

### 4.3 Simplified Causal Model

Equation 4 is the ideal modeling objective to train our model on since it allows us to exactly assign utility to each type of user we encounter. Unfortunately, the type of the user is latent and only can be estimated with bounds, as is discussed in [7]. Theoretically, we could infer the user type by running a variety of experiments to disable/enable the non-native section for a user in order to measure the effect. Practically, we have limited data availability which constrains our ability to infer user type.

Instead of attempting to infer the above terms (e.g.  $P(y_x, y'_{x'})$ ), we focus our efforts on a more manageable term:  $P(y_x|y')$ , the probability that, observed on  $y'$ , Y would be  $y$  if we have  $x$ . In other words, if we observed that a user has no click to the non-native link, the probability that this user would click the non-native link if we *had* shown the non-native link. We could then use this proxy objective function:

$$\alpha * \text{click} - \text{keypress} + \beta * P(y_x|y') \quad (5)$$

The final included term  $P(y_x|y')$  has two benefits:

- we will only turn off users who previously had the non-native section enabled and did not click.
- newly turn on user has higher probability to click on non-native link.

**4.3.1 Computing a practical bound.** Since  $P(y_x|y')$  is still intractable and cannot actually be computed, we need to find a way to evaluate this term by the available data.

<sup>2</sup>Previous work which classified users into these response types used examples of targeting advertisement to a user – defier in this setting would make more intuitive sense, but can be ignored in this scenario.

We can bound  $P(y_x|y')$  as following:

$$P(y_x|y') = \frac{P(y_x, y')}{P(y')} \geq \frac{[P(y_x) - P(y)]}{P(y')}$$

Although we have the data for  $P(y_x)$  (experimental data), we do not have  $P(y)$ , as it is observational data. We can also infer  $P(y)$  with a proxy variable  $w$  - denoting whether or not that a user has Drive activity. We have  $P(y) = P(w, y) + P(w', y) = P(w, y)$ , because if we have non-native click, we must have Drive activity, thus:

$$P(y_x|y') \geq \frac{[P(y_x) - P(y)]}{P(y')} = \frac{[P(y_x) - P(w, y)]}{P(y')} \geq \frac{[P(y_x) - P(w)]}{1} \quad (6)$$

**4.3.2 Group-level to user-level objective function.**  $P(y_x|y')$  is clearly a group-level term, i.e. for a group of users, we can evaluate this term among the group, and all users in the group have the same value of  $P(y_x|y')$ . It means given some training data with  $n$  users, we can only identify a group of  $m < n$  users that maximize the objective function. However, in an ML model that is serving live traffic, we need to be able to have a user-level decision for whether or not to serve the non-native section, rendering the group-level objective function we derived to be non-trivial to apply.

Given that there are  $2^n$  subsets of the users, there is at least one subset that maximize  $P(y_x|y')$ . We postulate that whether or not a user is in the desired subset is partially determined by the users attributes. Our methodology consists of finding the subset of users to maximize the group-level objective function defined in Equation 6, and then taking their group membership into account into the training loss function. In other words, if we provide a 0/1 label indicating whether the user is in the desired subset to the ML model, the training process would have additional information to be able to exploit the relation between the user attributes with this counterfactual logic.

Therefore, we modified our model training process to use the following objective function in place of Equation 1:

$$\alpha * \text{click} - \text{keypress} + \beta * \Phi[\text{member}] \quad (7)$$

where  $\Phi[\text{member}]$  is an indicator function that returns 1 iff the user is in the group that maximize  $P(y_x|y')$  and 0 otherwise.

**4.3.3 Group determination method.** We need a simple closed-form labeling method that can determine a group of users that comes close to maximizing Equation 6. Let  $a$  be the number of users have non-native click,  $b$  be the number of users have non-native link,  $c$  be the number of users have Drive activity, and  $n$  be the number of users. Then we have:

$$P(y_x) - P(w) = \frac{a}{b} - \frac{c}{n}$$

The key insight here is that if we add a user with non-native click and Drive activity, it depends on the relation of the proportion of  $a$  in  $b$  and the proportion of  $c$  in  $n$ . We propose the group determination method shown in Figure 2, as it is the simplest condition

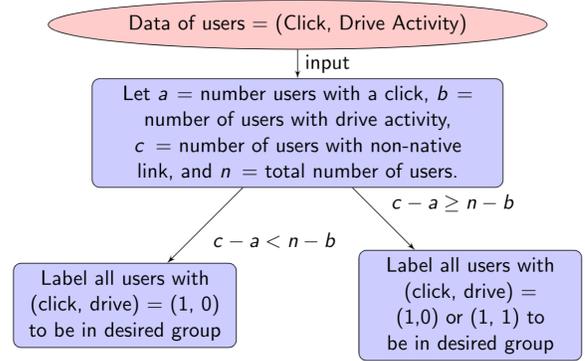


Figure 2: Group determination method

to make  $P(y_x) - P(w)$  larger, because if (click,drive) = (1, 0), we have the following:

$$(P(y_x) - P(w))_{\text{new}} - (P(y_x) - P(w))_{\text{old}} = \frac{a+1}{b} - \frac{c+1}{n+1} - \left(\frac{a}{b} - \frac{c}{n}\right) = \frac{n^2 + n - nb + c}{bn(n+1)} \geq 0$$

and if (click,drive) = (1, 1) and  $(c - a \geq n - b)$ , we have the following:

$$(P(y_x) - P(w))_{\text{new}} - (P(y_x) - P(w))_{\text{old}} = \frac{a+1}{b+1} - \frac{c+1}{n+1} - \left(\frac{a}{b} - \frac{c}{n}\right) = \frac{b-a}{b(b+1)} - \frac{n-c}{n(n+1)} \geq 0$$

## 4.4 Experimental Results

We ran experiments to compare the standard ML model that is used in production against the causal-trained model. We trained a model using the objective function defined in Equation 7 and compared it to the normal ML-model (which was trained with the objective function defined in Equation 1). We ran a week-long experiment and found that the causal-trained model led to to 9.15% increase in non-native click-through rate (CTR) with a non-significant increase of 1.4% in terms of resource usage.

This is a significant improvement – to contrast this with previous improvements, we previously saw that the initial deployment of the first machine-learned model led to 2.5% relative increase in non-native click-through rate (CTR) with a further saving of -6.5% resource saving.

## 5 CONCLUSION AND FUTURE WORK

We introduced a novel method in which we can incorporate causal information into the training process for a real-world binary classification problem. Additionally, we demonstrate that we see empirical wins from using this method in live traffic experiments. For future work planned is to prove theoretically that such methods are robust and can be reproduced in various other domains.

## REFERENCES

- [1] Joshua D Angrist, Guido W Imbens, and Donald B Rubin. 1996. Identification of causal effects using instrumental variables. *Journal of the American statistical Association* 91, 434 (1996), 444–455.
- [2] Alexander Balke and Judea Pearl. 1997. Bounds on treatment effects from studies with imperfect compliance. *J. Amer. Statist. Assoc.* 92, 439 (1997), 1171–1176.
- [3] Léon Bottou, Jonas Peters, Joaquin Quiñero-Candela, Denis X Charles, D Max Chickering, Elon Portugaly, Dipankar Ray, Patrice Simard, and Ed Snelson. 2013. Counterfactual reasoning and learning systems: The example of computational advertising. *The Journal of Machine Learning Research* 14, 1 (2013), 3207–3260.
- [4] David Galles and Judea Pearl. 1998. An axiomatic characterization of causal counterfactuals. *Foundations of Science* 3, 1 (1998), 151–182.
- [5] Joseph Y Halpern. 2000. Axiomatizing causal reasoning. *Journal of Artificial Intelligence Research* 12 (2000), 317–337.
- [6] Shin-Yuan Hung, David C Yen, and Hsiu-Yu Wang. 2006. Applying data mining to telecom churn management. *Expert Systems with Applications* 31, 3 (2006), 515–524.
- [7] Ang Li and Judea Pearl. 2019. Towards a White Box Approach to Automated Algorithm Design. In *Proceedings of the Twenty-Eighth International Joint Conference on Artificial Intelligence (IJCAI'19)*.
- [8] Lihong Li, Shunbao Chen, Jim Kleban, and Ankur Gupta. 2015. Counterfactual estimation and optimization of click metrics in search engines: A case study. In *Proceedings of the 24th International Conference on World Wide Web*. ACM, 929–934.
- [9] Judea Pearl. 1995. Causal diagrams for empirical research. *Biometrika* 82, 4 (1995), 669–688.
- [10] Judea Pearl. 2009. *Causality*. Cambridge university press.
- [11] Wei Sun, Pengyuan Wang, Dawei Yin, Jian Yang, and Yi Chang. 2015. Causal Inference via Sparse Additive Models with Application to Online Advertising.. In *AAAI*. 297–303.
- [12] Chih-Fong Tsai and Yu-Hsin Lu. 2009. Customer churn prediction by hybrid neural networks. *Expert Systems with Applications* 36, 10 (2009), 12547–12553.
- [13] Lidan Wang, Jimmy Lin, and Donald Metzler. 2011. A cascade ranking model for efficient ranked retrieval. In *Proceedings of the 34th international ACM SIGIR conference on Research and development in Information Retrieval*. ACM, 105–114.
- [14] Jun Yan, Ning Liu, Gang Wang, Wen Zhang, Yun Jiang, and Zheng Chen. 2009. How much can behavioral targeting help online advertising?. In *Proceedings of the 18th international conference on World wide web*. ACM, 261–270.